

Welcome to

# Electric Machines & Drives

thomasblairpe.com/EMD

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**Session 7:  
 Synchronous Motors  
 & Generators**

Fall 2011



## Session 7

- Chapter 16 – Synchronous Generators
- Chapter 17 – Synchronous Motors

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## Chapter 16 – Synchronous Generators

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## Chapter 16

Stationary Field generator < 5kva  
 stationary field – rotating armature  
 slip ring connection to armature

Rotating Field generator (alternator) > 5kva  
 stationary armature – rotating field  
 slip ring connection to field

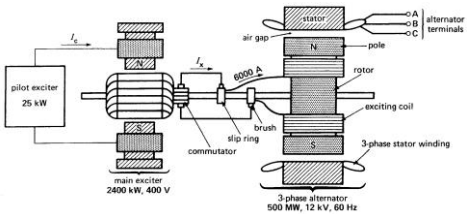
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## Chapter 16

### DC generator for field generation of Synchronous Generator



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One complete cycle every time pole pair passed ->

Frequency generated is:  
 $f = p n / 120$

$f$  = frequency of the induced voltage (Hz)  
 $p$  = number of poles on rotor  
 $n$  = speed of the rotor (rpm)

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**Example 16-1**

A hydraulic turbine turning at 200 rpm is connected to a synchronous generator. If the induced voltage has a frequency of 60 Hz, how many poles does the rotor have?

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Stator Features: Identical to 3 phase motor  
Stacked laminations  
Always connected in wye for following reasons:

- Voltage per coil 58% line voltage
- Third harmonic voltages cancel (same in each phase), in delta they add and cause circulating current.
- Max term voltage typically 25kv.

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Rotor Features:  
High speed slotted cylindrical forging  
Smaller diameter – centrifugal forces  
Longer to get air gap area needed for power  
Retaining ring – insulated  
Low speed typically salient pole  
Larger diameter – lower speed – more poles  
Shorter due to more air gap area per foot length  
Coils in series (mica strip insulation)  
Squirrel cage in pole faces (damper winding) for transient dampening

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Field Excitation - typically .5% to 2% machine rating

Two functions

1. maintain ac line voltage
2. provide reactive power to system

Slip ring and Brush exciter

1. provided by DC generator on same shaft
2. Provided by MG set separately driven
3. Provided by separate sourced solid state rectifier

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Brushless exciter

1. Provided by PMG same shaft via separate sourced solid state rectifier to alternator on shaft
2. Provided by external source via solid state rectifier to alternator on shaft.

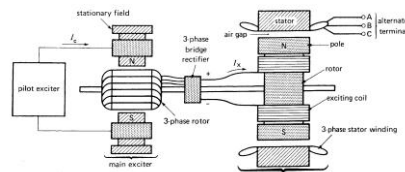
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Brushless exciter – Less maintenance  
Ic controls field current  
Frequency > main frequency



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Size of synchronous generators:  
 Larger size -> higher efficiency  
 Power per KG greater (more power per \$)  
 Cooling of large machines challenge  
 Indirectly cooled winding  
 Gas intercooled winding  
 Water cooled winding

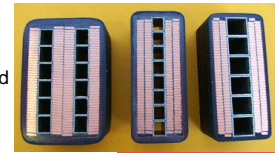
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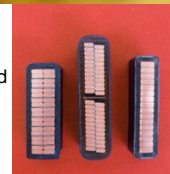
Gas intercooled



Water intercooled



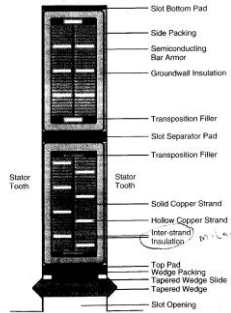
Indirectly Cooled



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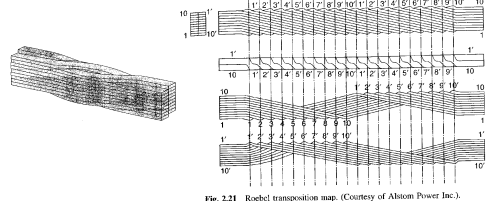
Strand insulation –  
 reduce eddy current  
 in conductor



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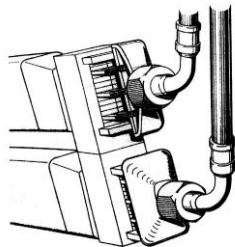
Robel Transposition – equalize magnetic  
 reactance of each conductor



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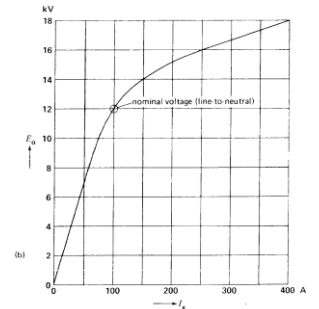
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Connection to liquid cooling system.



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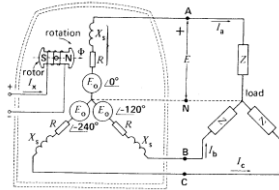
No Load  
 Saturation  
 Curve



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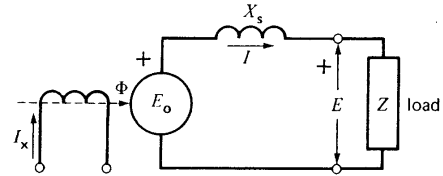
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Resistive element & Inductive element  
 $X \gg R$   
 Simplify by neglect R



### Chapter 16

Simplified SLE circuit for Synchronous Generator



### Chapter 16

Synchronous Reactance

$$X_s = 2 \pi f L$$

$X_s$  = Synchronous reactance per phase ( $\Omega$ )

$f$  = generator frequency (Hz)

$L$  = apparent inductance of stator winding per phase

### Chapter 16

Measurement of  $X_s$

Open circuit test – rated speed and open terminals, excitation raised to meet rated  $V$  ( $E_n$ ). This is value of ( $I_{xn}$ )

Short Circuit test – rated speed and shorted terminals, excitation raised back to  $I_{xn}$ , and armature current measured (value of  $I_{sc}$ )

### Chapter 16

$$X_s = E_n / I_{sc}$$

$X_s$  = synchronous reactance pwer phase ( $\Omega$ )

$E_n$  = rated open circuit line to neutral voltage (V)

### Example 16-2

A 3 phase synchronous generator produces an open circuit line voltage of 6928 V when the dc exciting current is 50A. The ac terminals are then short circuited and the three line currents are found to be 800A. Calculate;

- The synchronous reactance per phase
- The terminal voltage if three  $12 \Omega$  resistors are connected in wye across the terminals.

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Base impedance –  
Use rated LINE TO NEUTRAL voltage ( $E_b$ )  
and rated power (S) PER PHASE

$$Z_b = E_b^2 / S_b$$

$Z_b$  = base impedance (line to neutral) of the generator ( $\Omega$ )

$E_b$  = base voltage (line to neutral (V))

$S_b$  = base power per phase (VA)

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**Example 16-3**

A 30 MVA, 15kV, 60 Hz ac generator has a synchronous reactance of 1.2 pu and a resistance of 0.02 pu. Calculate

- The base voltage, base power and base impedance of the generator
- The actual value of the synchronous reactance
- The actual winding resistance, per phase
- The total full load copper losses

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Short Circuit Ratio (SCR) –  
Ratio of  $I_{x1}$  to  $I_{x2}$ , where  $I_{x1}$  is field current to produce nominal open circuit voltage and  $I_{x2}$  is field current to produce nominal armature current on short circuited terminals (steady state)

$$X_s \text{ (pu)} = (I_{x2} / I_{x1}) = 1/\text{SCR}$$

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Generator supplying lagging load - Lagging PF,  
 $I$  leads  $E$ ,  
 $E(X_s)$  leads  $I$  by 90 degrees,  
 $E_o = E + E_x$ , therefore  $E_o > E$ ,  
Angle between  $E$  and  $E_o$  is power angle ( $\delta$ )

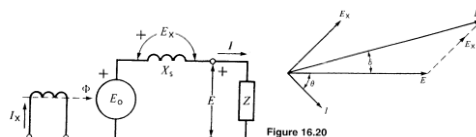


Figure 16.20  
Phasor diagram for a lagging power factor load.



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Generator supplying leading load - Leading PF,  
 $I$  lags  $E$ ,  
 $E(X_s)$  leads  $I$  by 90 degrees,  
 $E_o = E + E_x$ , therefore  $E_o < E$ ,  
Angle between  $E$  and  $E_o$  is power angle ( $\delta$ )  
Note same power angle as before.

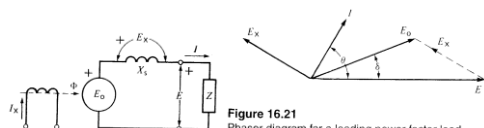


Figure 16.21  
Phasor diagram for a leading power factor load.



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**Example 16-4**

A 36 MVA, 20.8 kV, 3 phase alternator has a synchronous reactance of 9  $\Omega$  and a nominal current of 1 kA. The no load saturation curve giving the relationship between  $E_o$  and  $I_x$  is given in Fig 16.13b. If the excitation is adjusted so that the terminal voltage remains fixed at 21 kV, calculate the exciting current required and draw the phasor diagram for the following conditions;

- No load
- Resistive load of 36 MW
- Capacitive load of 12 Mvar

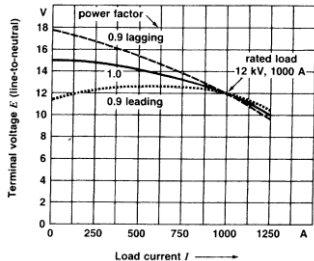
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Voltage regulation vs. load PF  
Eo Fixed at rated load



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Percent Regulation is defined as:

$$\% \text{ regulation} = 100\% (E_n - E_b) / E_b$$

$E_n$  = no load voltage (V)

$E_b$  = rated voltage (V)

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**Example 16-5**

Generator Synchronization:

1. Generator Frequency = System Frequency (preferred slightly faster) WHY?
2. Generator Voltage Magnitude = System Voltage Magnitude (preferred slightly higher) WHY?
3. Generator Voltage Phase Angle = System Voltage Phase Angle (breaker closing time added to calculation)
4. Generator Phase sequence = System Phase Sequence

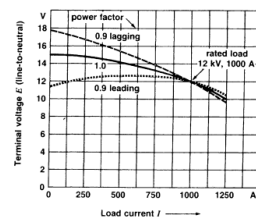
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Calculate the percent regulation corresponding to the unity power factor curve in figure below.



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Infinite Bus Characteristics:

1. Adjusting excitation adjusts  $E_o$  – controls VAR flow.
2. Adjusting mechanical torque adjusts power angle  $\delta$  – control watts flow.

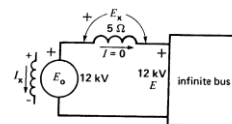
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Zero current,  $E$  in phase with  $E_o$



**Figure 16.26a**  
Generator floating on an infinite bus.

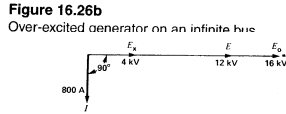
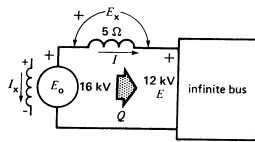
$$E_o = E = 12 \text{ kV}$$



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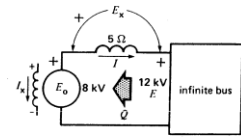
Overexcited  
System looks like  
Inductive Load –  
I lags E  
Ex in phase with  
E  
E + Ex = Eo  
Var transfer to  
system



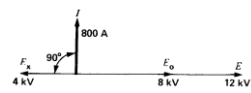
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Under excited  
System looks  
like Capacitive  
Load –  
I leads E  
Ex 180° out of  
phase with E  
E + Ex = Eo  
Var transfer to  
generator



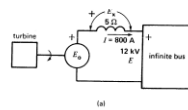
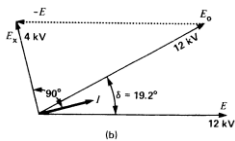
**Figure 16.26c**  
Under-excited generator on an infinite bus.



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Increasing Torque,  
Eo advances ahead of E,  
increased power angle  $\delta$ ,  
NOTE: even though E and Eo have same magnitude  
(implying no VAR transfer) power is still transferred  
due to power angle  $\delta$



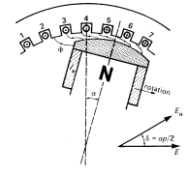
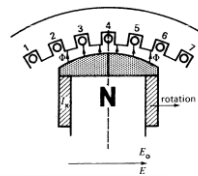
**Figure 16.27**  
a. Turbine driving the generator.  
b. Phasor diagram showing the torque angle  $\delta$ .



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Rotor Position – no load to full load –  
Torque by prime mover advances rotor  
position



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Mechanical angle of rotor pole to stator pole  
related to power angle by: (Note for 2 pole  
generator,  $\alpha = \delta$  )

$$\delta = \alpha (p/2)$$

$\delta$  = torque angle between the terminal voltage E  
and excitation voltage Eo (electrical degrees)  
P = number of poles on generator  
 $\alpha$  = mechanical angle between the centers of  
the stator and rotor poles (mechanical degrees)

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**Example 16-6**

The rotor poles of an 8 pole synchronous  
generator shift by 10 mechanical degrees from  
no load to full load.

- Calculate the torque angle between Eo and the terminal voltage E at full load.
- Which voltage, E or Eo is leading?

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For Proof of equation, see web site;  
[http://www.thomasblairpe.com/EMD/PPE/PWR\\_XFER.pdf](http://www.thomasblairpe.com/EMD/PPE/PWR_XFER.pdf)

$$P = [(E_o E) / X_s] \sin \delta$$

P = active power per phase (W)  
 E<sub>o</sub> = induced voltage per phase (V)  
 E = terminal voltage per phase (V)  
 δ = torque angle between E<sub>o</sub> and E (Degrees)

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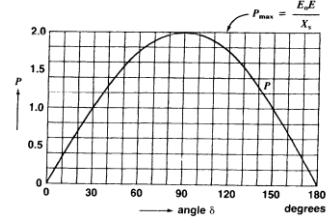


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Rated power typically around 30° – Power angle > 90° cause pole slip and out of synch condition.

Curve different for salient pole machine



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### Example 16-7

A 36 MVA, 21kV, 1800 rpm, 3 phase generator connected to a power grid has a synchronous reactance of 9 Ω per phase. If the exciting voltage is 12 kV (line to neutral) and the system voltage is 17.3 kV (line to line), calculate the following:

- The active power which the machine delivers when the torque angle δ is 30° (electrical)
- The peak power that the generator can deliver before it falls out of step.

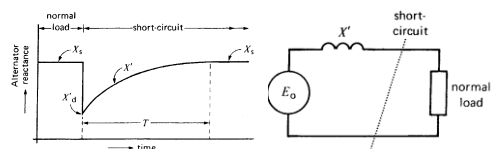
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Transient reactance vs synchronous reactance  
 0.15PU typical – breaker interrupt capability – better voltage regulation during transient



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### Example 16-8

A 250 MVA, 25 kV, 3 phase steam turbine generator has a synchronous reactance of 1.6 pu and a transient reactance X'd of 0.23 pu. It delivers its rated output at a power factor of 100%. A short circuit suddenly occurs on the line, close to the generating station. Calculate

- The induced voltage E<sub>o</sub> prior to the short
- The initial value of the short circuit current
- The final value of the short circuit current if the circuit breakers should fail to open.

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Power flow between 2 machines:  
 Power flow from leading voltage to lagging voltage (regardless of magnitude)

$$P = [(E_1 E_2) / X] \sin \delta$$

P = active power transmitted (W)  
 E<sub>1</sub> = voltage of source 1 (V)  
 E<sub>2</sub> = voltage of source 2 (V)  
 δ = torque angle between E<sub>1</sub> and E<sub>2</sub> (Degrees)

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$P = [(E_1 - E_2) / X] \sin \delta$

(a) (b)

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Referring to fig. 16.33a, source A generates a voltage  $E_1 = 20 \text{ kV} / \angle 5^\circ$  and source B generates a voltage  $E_2 = 15 \text{ kV} / \angle 42^\circ$  and source. The transmission line connecting them has an inductive reactance of  $14 \Omega$ . Calculate the active power that flows over the line and specify which source is actually a load.

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As machine size increases, efficiency increases  
Larger machines produce more power / KG material (\$)  
Temperature rise challenge – cooling more complex

$\eta = 100\% (P_o/P_i)$

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Coil installation:

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Coils may be series or parallel

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2 pole machines oscillate at 2X line frequency – core mounting absorbs vibration

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**Chapter 16**  
**Cylindrical Rotor Construction**

The top left diagram shows an axial cooled rotor winding with labels: Rotor Tooth, Creepage Block, Rotor Wedge, Slot Liner, Copper Winding, Interturn Insulation, Axial Vent, and Slot Separator. The top right diagram shows a radial cooled rotor winding with subslots, with labels: Rotor Tooth, Creepage Block, Rotor Wedge, Slot Liner, Copper Winding, Interturn Insulation, Radial Vent, and Subslot. The bottom diagram is a cross-section of a cylindrical rotor with labels: Coupling, Axial Fan, Interlocking Ring, End-winding, Bearing Journal, Excitation End, Slip Rings, Winding Slot Wedges, and Bearing Journal Drive End.

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**Chapter 16**  
**Bore Copper and terminal stud connector for DC field circuit**

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**Chapter 16**  
**Typical Brush gear for DC field circuit**

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**Chapter 16**  
**Typical hydrogen seal –  $P_{oil} > P_{hydrogen}$**

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Labels in the diagram include: Inboard Seal, Machine Seal, Spherical Seat, Sleeve Bearing, Oil Filler, Outboard Seal, Lubrication Ring, Oil Reservoir, Oil Sight Cage, Oil Drain, Pressure Equalization, and Sight Gage.

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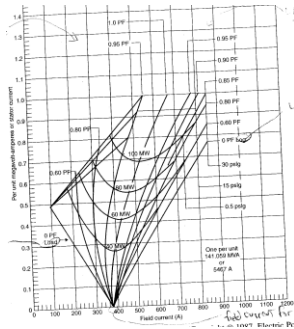
**Chapter 16**  
**Generator Capability Curve**

The graph plots Leading and Lagging MVA on the y-axis (from -100 to 120) against MVA on the x-axis (from 0 to 180). It shows constant power factor (PF) lines from 0.70 to 0.95. Limitations include: 'Limited by stator core heating and field heating' at the top; 'Limited by rotor heating' on the right; 'Limited by cooling, heating, stator and winding heating, and minimum excitation' at the bottom; and 'Stability limit for voltage regulator' on the right side.

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**Chapter 16**

V-Curve –  
Apparent power  
to Field current  
for various  
power loading



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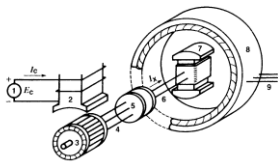
**Chapter 17 – Synchronous Motors**



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**Chapter 17**

Construction similar to Synchronous Generator  
Stator slotted wedges  
Rotor Salient Poles – damper winding imbedded in pole face



- 1 - dc control source
- 2 - stationary exciter poles
- 3 - alternator (3-phase exciter)
- 4 - 3-phase connection
- 5 - bridge rectifier
- 6 - dc line
- 7 - rotor of synchronous motor
- 8 - stator of synchronous motor
- 9 - 3-phase input to stator



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**Example 17-1**

Calculate the number of salient poles on the rotor of the synchronous motor rated at 4000 HP (3000 kW), 200 rpm, 6.9 kV, 60 Hz, 80% power factor. The brushless exciter is rated at 50 kW, 250 V.



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**Chapter 17**

Starting Synchronous motor – amortisseur winding  
Short field winding during start - Limit induced voltage on field winding & improve starting torque  
Also reduced voltage start or pony motor start  
VFD also used for starting very large synchronous motor (and combustion turbine generators)



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**Chapter 17**

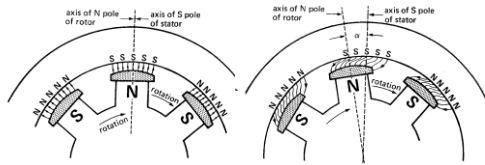
Pull in torque – Applying DC to field generates field – pulls rotor into synch with stator field (pull in torque)  
Detection of position of rotor pole position important  
When in synch, amortisseur winding sees no slip -> no voltage induced in winding



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As Load increase  $\alpha$  increases. Pull out torque, value at which poles slip. Value depends on mmf of rotor and stator – depend on field and armature current.



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**Chapter 17**

Motor under load calculations:

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**Chapter 17**

$E = E_x + E_o$

Note  $\delta$  still between E and  $E_o$ , but  $E_o$  now lags E (unlike generator)

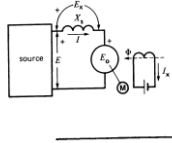


Figure 17.7b

Motor at no-load, with  $E_o$  adjusted to equal E.

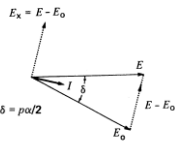


Figure 17.7c

Motor under load E, has the same value as in Fig. 17.7b, but it lags behind E.



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**Example 17-2a**

A 500 HP, 720 rpm synchronous motor connected to a 3980V, 3 phase line generates an excitation voltage  $E_o$  of 1790 V (line to neutral) when the dc exciting current is 25 A. The synchronous reactance is  $22 \Omega$  and the torque angle between  $E_o$  and E is  $30^\circ$ . Calculate;

- The value of  $E_x$
- The ac line current
- The power factor of the motor
- The approximate HP developed by the motor
- The approximate torque developed at the shaft.

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**Example 17-2b**

The motor in example 17-2a has a stator resistance of  $0.64 \Omega$  per phase and possesses the following losses:.

|                         |        |
|-------------------------|--------|
| $I^2R$ loss in rotor    | 3.2 kW |
| Stator iron loss        | 3.3 kW |
| Windage / friction loss | 1.5 kW |

Calculate

- The actual HP developed
- The actual torque developed at the shaft
- The efficiency of the motor.

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**Chapter 16**

Power & Torque

$P = [(E_o E) / X_s] \sin \delta$

$P_{max} = (E_o E) / X_s$

$P$  = mechanical power of motor per phase (W)

$E_o$  = line to neutral voltage induced by  $I_x$  (V)

$E$  = line to neutral voltage of source (V)

$X_s$  = synchronous reactance per phase ( $\Omega$ )

$\delta$  = torque angle between  $E_o$  and E (Degrees)

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**Chapter 16**

Power & Torque

$$T = 9.55 P / ns$$

T = torque per phase (N m)

P = mechanical power per phase (W)

ns = synchronous speed (rpm)

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**Example 17-3**

A 150 kW, 1200 rpm, 460V 3 phase synchronous motor has a synchronous reactance of  $0.8 \Omega$  per phase. If the excitation voltage  $E_o$  is fixed at 300V per phase, determine the following:

- The power versus  $\delta$  curve
- The torque versus  $\delta$  curve
- The pull out torque of the motor

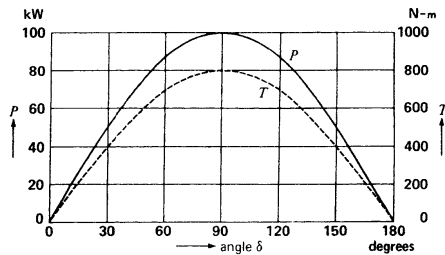
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**Example 17-3**

Solution

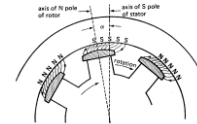
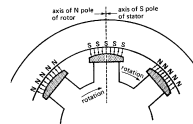


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**Chapter 17**

Relationship between power angle  $\delta$  and mechanical angle  $\alpha$  between stator and rotor pole centers  
Same as Generator – also note for 2 pole machine,  $\alpha = \delta$

$$\delta = \alpha (p/2)$$



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**Example 17-4**

A 3 phase, 6000 kW, 4kV, 180 rpm, 60 Hz motor has a synchronous reactance of  $1.2 \Omega$ . At full load the rotor poles are displaced by a mechanical angle of  $1^\circ$  from their no load position. If the line to neutral excitation  $E_o = 2.4$  kV, calculate the mechanical power developed.

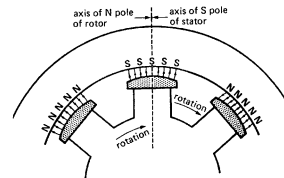
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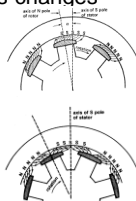
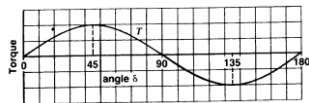
The flux produced by the stator flows across the air gap through the salient poles



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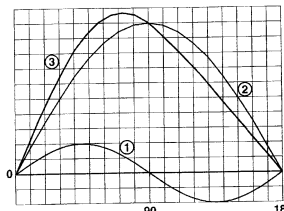
**Chapter 17**

Reluctance torque for salient pole machine –  
As power angle  $\delta$  increases, concentration of flux between rotor and stator poles changes  
This variation in flux leads to variation in torque (known as reluctance torque)



**Chapter 17**

Resultant Torque  
1 – Reluctance Torque  
2 – Cylindrical Torque  
3 – Resultant Torque  
PEAK – 70°



**Chapter 17**

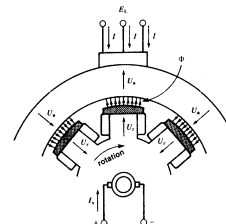
Large Vs Small Synchronous Motor characteristic

1.  $\delta$  ranges from 27° to 37°
2. Excitation power (per unit) smaller for larger machine
3. Improved efficiency for larger motor
4.  $X_s \gg R_s$  – simplified SLE model

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**Chapter 17**

Excitation & Reactive Power  
Controlling  $I_x$ , controls flux in motor,  
If flux < needed, motor absorbs reactive power from line  
If flux > needed, motor delivers reactive power to line.



**Chapter 17**

Power Factor Rating – Motor rated PF allows motor to deliver reactive power without derate of motor active power. Motor larger for lower PF rating

$P = E_{ab} I_p$



Figure 17.14  
Unity power factor synchronous motor and phasor diagram at full-load.

**Chapter 17**

Motor with 80% power factor  
 $I_p$  – contributes to active power to load  
 $I_q$  – contributes to reactive power to system  
 $I_p = 0.8 I_s$   
 $I_q = 0.6 I_s$   
 $Q = E_{ab} I_q$   
 $= 0.6 E_{ab} I_s$   
 $P = E_{ab} I_p$   
 $= 0.8 E_{ab} I_s$



Figure 17.15  
80 percent power factor synchronous motor and phasor diagram at full-load.

## Chapter 17

V-curves:

If we reduce  $I_x$  below that needed for unity power, motor draws reactive power  
 If we increase  $I_x$  above that needed for unity power, motor provides reactive power

$$S = \sqrt{P^2 + Q^2}$$

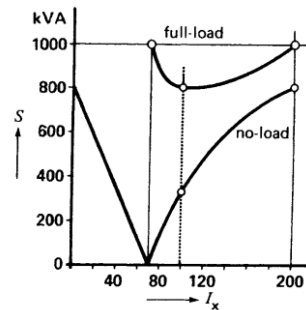
-> S minimum at PF = 1.0, increases for either increasing or decreasing excitation current

Shown on V-Curve

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## Example 17-5

A 4000 HP (3000 kW), 6600V, 60 Hz, 200 rpm synchronous motor operates at full load at leading power factor of 0.8. If the synchronous reactance is  $11 \Omega$ , calculate the following:

- The apparent power of the motor, per phase
- The ac line current
- The value and phase of  $E_o$
- Draw the phasor diagram
- Determine the torque angle  $\delta$

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## Chapter 17

Stopping Synchronous Motor –

Following methods:

- Coasting (may take time to come to rest)
- Break by maintain full DC excitation with Armature short circuit (dynamic braking)
- Break by maintain full CD excitation with Armature connected to resistor bank (dynamic braking)
- Apply mechanical break

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## Example 17-6

A 1500 kW, 4600V, 600 rpm, 60 Hz synchronous motor possesses a synchronous reactance of  $16 \Omega$  and a stator resistance of  $0.2 \Omega$  per phase. The excitation voltage  $E_o$  is 2400V and the moment of inertia of the motor and its load is  $275 \text{ kg m}^2$ . We wish to stop the motor by short circuiting the armature while keeping the dc rotor current fixed.

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## Example 17-6

Calculate

- The power dissipated in the armature at 600 rpm
- The power dissipated in the armature at 150 rpm
- The kinetic energy at 600 rpm
- The kinetic energy at 150 rpm
- The time required for the speed to fall from 600 rpm to 150 rpm.

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**Chapter 17**

Synchronous motor vs induction motor –  
 Low Speed – Synchronous machine efficiency  
 higher (near rated load) and PF adjust to 1.0  
 Can provide reactive power to plant for voltage  
 support  
 Starting Torque Higher for synchronous motor

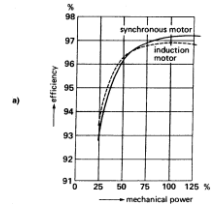
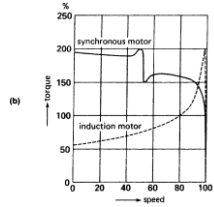
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**Chapter 17**

Comparison between the efficiency and starting  
 torque of induction and synchronous motor



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**Example 17-7**

A synchronous capacitor is rated at 160 Mvar,  
 16 kV, 1200 rpm, 60 Hz. It has a synchronous  
 reactance of 0.8 pu and is connected to a 16  
 kV line. Calculate the value of  $E_o$  so that the  
 machine  
 a. Absorbs 160 Mvar  
 b. Delivers 120 Mvar

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**Chapters 18 and 19 next session**



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End of Session 7:  
 Synchronous Motors  
 & Generators

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